

Expected Constant Round Byzantine Broadcast under Dishonest Majority

Jun Wan (junwan@mit.edu)

Hanshen Xiao (hsxiao@mit.edu)

Elaine Shi (runting@gmail.com)

Srini Devadas (devadas@csail.mit.edu)

Byzantine Broadcast [Lamport et al. 82]

- A set of users aim to reach consensus, one of them is the designated sender.
- The sender is given an input bit $b \in \{0, 1\}$
 - *Consistency*: all honest users must output the same bit; and
 - *Validity*: all honest users output the sender's input bit if the sender is honest.

Background and Previous Work

- Synchronous, assume trusted cryptographic setup
- [Dolev and Strong, 83]: no deterministic protocol can achieve Byzantine Broadcast within $f + 1$ rounds, where f is the number of corrupted users.
- Focus on randomized protocols

Previous work

- Honest majority: expected constant rounds protocols exist (even under adaptive adversary) [Katz and Koo 09, Abraham et al. 19].
- Dishonest majority:

Garay et al., 07 *Fitz et al. 09*

$$O((2f - n)^2) \qquad O((2f - n))$$



n : # total users

f : # corrupted users

Previous work

- Honest majority: expected constant rounds protocols exist (even under adaptive adversary) [Katz and Koo 09, Abraham et al. 19].
- Dishonest majority:

Garay et al., 07

$$O((2f-n)^2)$$

Fitz et al. 09

$$O(2f-n)$$



n: # total users

Chan et al. 20

f: # corrupted users

$\text{polylog}(n)$

Previous work

- Honest majority: expected constant rounds protocols exist (even under adaptive adversary) [Katz and Koo 09, Abraham et al. 19].
- Dishonest majority: **can we also achieve expected constant round complexity?**

Garay et al., 07

$$O((2f-n)^2)$$

Fitz et al. 09

$$O((2f-n))$$

Our result

$$O((n/(n-f))^2)$$



n : # total users

f : # corrupted users

Chan et al. 20

$\text{polylog}(n)$

Our results

- Round complexity: $\Theta((n/(n-f))^2)$.
- Tolerates adaptive adversary: cannot erase messages already sent upon corrupting the user

Garay et al., 07

Fitz et al. 09

Our result

$$O((2f-n)^2)$$

$$O((2f-n))$$

$$O((n/(n-f))^2)$$



n : # total users

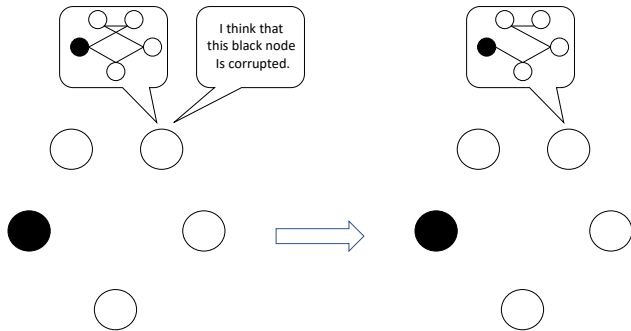
Chan et al. 20

f : # corrupted users

$\text{polylog}(n)$

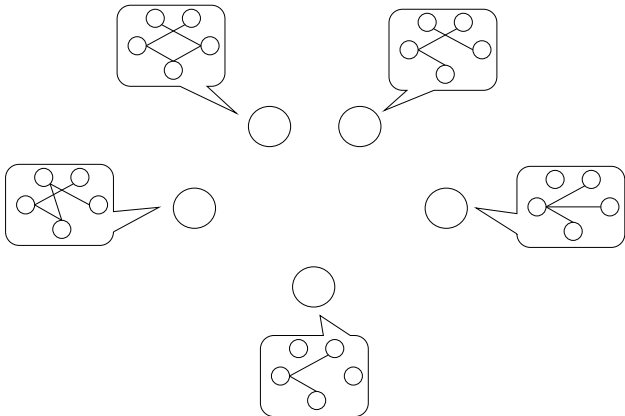
Novelty and new techniques

- Use a new graph idea: the trust graph.



Novelty and new techniques

- Use a new graph idea: the trust graph.



Novelty and new techniques

- Use a new graph idea: the trust graph.
- Build a new primitive and bootstrap full consensus from this weaker primitive, similar to gradecast.

Thank you

- Future work: strongly adaptive adversary
- See details of the paper on Eprint